Mustafa Jarrar: Lecture Notes on **Decision Trees Machine Leaning** Birzeit University, 2021



Machine Learning

Decision Trees Classification

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Acknowledgement: This lecture is based on (but not limited to) to the lecture notes found in [1,2,3] Mustafa Jarrar: Lecture Notes on Decision Trees Machine Leaning Birzeit University, 2021

Machine Learning **Decision Tree Classification**

In this lecture:



- **Part 1: Motivation Example**
- Part 2: ID3 Algorithm
- Part 3: Entropy and Information Gain
- Part 4: Overfitting and Pruning
- □ Part 5: Classifying Continuous/Numerical Values
- Part 6: Pros and Cons of Decision Trees
- □ Part 7: Using R and Python to learn Decision Trees

Example of a Decision Tree

Is it a good weather to play outside?



How to learn such a tree from past experience?

Given the following training examples, will you play in D15?

Divide and conquer:

- split into subsets
- are they pure?
 - (all yes or all no)
- if yes: stop
- if not: repeat

See which subset new data falls into

Day	Outlook	Humidity	Wind	Plav
D1	Sunny	High	Weak	No
D2	Sunny	High	Strong	No
D3	Overcast	High	Weak	Yes
D4	Rain	High	Weak	Yes
D5	Rain	Normal	Weak	Yes
D6	Rain	Normal	Strong	No
D7	Overcast	Normal	Strong	Yes
D8	Sunny	High	Weak	No
D9	Sunny	Normal	Weak	Yes
D10	Rain	Normal	Weak	Yes
D11	Sunny	Normal	Strong	Yes
D12	2 Overcast	High	Strong	Yes
D13	Overcast	Normal	Weak	Yes
D14	a Rain	High	Strong	No
New data				
D1	5 Rain	High	Weak	???
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Training Examples









Decision Rule:

 $Yes \Leftrightarrow (Outlook=Overcast) \lor \\ (Outlook=Sunny \land Humidity=Normal)\lor \\ (Outlook=Rain \land Wind=Weak)$

Day Outlook Humid Wind D15 Rain High Weak ???

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Play

Decision Trees are Interpretable



Disjunction of conjunctions of constraints on the attribute values of instances i.e., $(... \land ... \land ...) \lor (... \land ... \land ...) \lor ...$

Set of **if-then-rules**, each branch represents one if-then-rule

- **if-part**: conjunctions of attribute tests on the nodes
- then-part: classification of the branch

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ID3 Algorithm

Split (node, {examples}):

- 1. A ← the <u>best attribute</u> for splitting the {examples}
- 2. Decision attribute for this node $\leftarrow A$
- 3. For each value of A, create new child node
- 4. Split training {examples} to child nodes
- 5. If examples perfectly classified: STOP

else: iterate over new child nodes

Split (child_node, {subset of examples})

- Ross Quinlan (ID3:1986), (C4.5:1993) from machine learning
- Breimanetal (CaRT:1984) from statistics

ID3 Algorithm



C4.5 (and C5.0) are similar algorithms to construct decision trees but are also able handle continuous values

In case of **Continuous Variables** like age, weight etc?



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Which attribute to split on?



Want to measure "purity" of the split

- more certain about Yes/No after the split
 - pure set (4 yes / 0 no) => completely certain (100%)
 - impure (3 yes / 3 no) => completely uncertain (50%)

- can't use the probability of "yes" given the set, P("yes" | set):
• must be symmetric: 4 yes / 0 no as pure as 0 yes / 4 no

Entropy

Entropy tells us how much a set of data is pure/impure For binary classification:

Entropy(S) = $H(S) = -p_{\oplus} \log_2 p_{\oplus} - p_{\ominus} \log_2 p_{\ominus}$ bits

- -S ... is a sample training examples
- $-p_{\oplus}$ proportion of positive examples in S
- $-p \ominus$ proportion of negative examples in S

 $-p_{\oplus}/p_{\ominus} \dots \%$ of positive/negative examples in S

- impure (3 yes / 3 no): $H(S) = -\frac{3}{6}\log_2\frac{3}{6} - \frac{3}{6}\log_2\frac{3}{6} = 1 \text{ bits}$
- pure set (4 yes / 0 no): $H(S) = -\frac{4}{4} \log_2 \frac{4}{4} - \frac{0}{4} \log_2 \frac{0}{4} = 0$ bits





Entropy tells us how much a set of data is pure/impure



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Information Gain

Entropy measures purity at each node, information gain looks at all nodes together and the expected drop in entropy after split.

Gain(S,A) = expected reduction in entropy due to sorting on A

 $Gain(S, A) = Entropy(S) - \sum_{v \in Values(A)} \frac{|Sv|}{S} \cdot Entropy(S_v)$

Maximum Gain(S, A) is selected!





 $Entropy(\text{Humidity}) = -9/14 \cdot \log_2(9/14) - 5/14 \cdot \log_2(5/14) = 0.94$ $Entropy(\text{High}) = -3/7 \cdot \log_2(3/7) - 4/7 \cdot \log_2(4/7) = 0.98$ $Entropy(\text{Normal}) = -6/7 \cdot \log_2(6/7) - 1/7 \cdot \log_2(1/7) = 0.59$

$$Gain(S, A) = Entropy(S) - \sum_{v \in \{\text{High, Normal}\}} \frac{|Sv|}{S} \cdot Entropy(S_v)$$

Gain(S, Humidity) = $0.94 - (7/14) \cdot 0.98 - (7/14) \cdot 0.59 = 0.151$

Day	<u>Outlook</u>	Humidity	Wind	<u>Play</u>
D1	Sunny	High	Weak	No
D2	Sunny	High	Strong	No
D3	Overcast	High	Weak	Yes
D4	Rain	High	Weak	Yes
D5	Rain	Normal	Weak	Yes
D6	Rain	Normal	Strong	No
D7	Overcast	Normal	Strong	Yes
D8	Sunny	High	Weak	No
D9	Sunny	Normal	Weak	Yes
D10	Rain	Normal	Weak	Yes
D11	Sunny	Normal	Strong	Yes
D12	Overcast	High	Strong	Yes
D13	Overcast	Normal	Weak	Yes
D14	Rain	High	Strong	No





 $Entropy(Outlook) = -9/14 \cdot \log_2(9/14) - 5/14 \cdot \log_2(5/14) = 0.94$ $Entropy(Sunny) = -2/5 \cdot \log_2(2/5) - 3/5 \cdot \log_2(3/5) = 0.97$ $Entropy(Overcast) = -4/4 \cdot \log_2(4/4) - 0/4 \cdot \log_2(0/4) = 0$ $Entropy(Rain) = -3/5 \cdot \log_2(3/5) - 2/5 \cdot \log_2(2/5) = 0.97$

 $Gain(S, Outlook) = 0.94 - (5/14) \cdot 0.97 - (4/14) \cdot 0 - (5/14) \cdot 97 = 0.247$

Day	<u>Outlook</u>	Humidity	<u>Wind</u>	<u>Play</u>
D1	Sunny	High	Weak	No
D2	Sunny	High	Strong	No
D3	Overcast	High	Weak	Yes
D4	Rain	High	Weak	Yes
D5	Rain	Normal	Weak	Yes
D6	Rain	Normal	Strong	No
D7	Overcast	Normal	Strong	Yes
D8	Sunny	High	Weak	No
D9	Sunny	Normal	Weak	Yes
D10	Rain	Normal	Weak	Yes
D11	Sunny	Normal	Strong	Yes
D12	Overcast	High	Strong	Yes
D13	Overcast	Normal	Weak	Yes
D14	Rain	High	Strong	No





 $Entropy(Wind) = -9/14 \cdot \log_2(9/14) - 5/14 \cdot \log_2(5/14) = 0.94$ $Entropy(Weak) = -6/8 \cdot \log_2(6/8) - 2/8 \cdot \log_2(2/8) = 0.81$ $Entropy(Strong) = -3/6 \cdot \log_2(3/6) - 3/6 \cdot \log_2(3/6) = 1$

 $Gain(S, Wind) = 0.94 - (8/14) \cdot 0.81 - (6/14) \cdot 1 = 0.048$

Day	<u>Outlook</u>	Humidity	Wind	<u>Play</u>
D1	Sunny	High	Weak	No
D2	Sunny	High	Strong	No
D3	Overcast	High	Weak	Yes
D4	Rain	High	Weak	Yes
D5	Rain	Normal	Weak	Yes
D6	Rain	Normal	Strong	No
D7	Overcast	Normal	Strong	Yes
D8	Sunny	High	Weak	No
D9	Sunny	Normal	Weak	Yes
D10	Rain	Normal	Weak	Yes
D11	Sunny	Normal	Strong	Yes
D12	Overcast	High	Strong	Yes
D13	Overcast	Normal	Weak	Yes
D14	Rain	High	Strong	No



The attribute with the largest Information Gain (Outlook 0.247) is selected as the decision node.

Nodes with zero Entropy (e.g., Overcast) does not need splitting



 $Entropy(\text{Humidity}) = -2/5 \cdot \log_2(2/5) - 3/5 \cdot \log_2(3/5) = 0.97$ $Entropy(\text{High}) = -0/3 \cdot \log_2(0/3) - 3/3 \cdot \log_2(3/3) = 0$ $Entropy(\text{Normal}) = -2/2 \cdot \log_2(2/2) - 0/2 \cdot \log_2(0/2) = 0$ $Gain(\text{S, Humidity}) = 0.97 - (3/5) \cdot 0 - (2/5) \cdot 0 = 0.97$



 $Entropy(Wind) = -2/5 \cdot \log_2(2/5) - 3/5 \cdot \log_2(3/5) = 0.97$ $Entropy(Weak) = -1/3 \cdot \log_2(1/3) - 2/3 \cdot \log_2(2/3) = 0.92$ $Entropy(Strong) = -1/2 \cdot \log_2(1/2) - 1/2 \cdot \log_2(1/2) = 1$ $Gain(S, Wind) = 0.97 - (3/5) \cdot 0.97 - (2/5) \cdot 1 = -0.012$

→ Outlook has the highest gain (0.97)



26)



 $Entropy(\text{Humidity}) = -3/5 \cdot \log_2(3/5) - 2/5 \cdot \log_2(2/5) = 0.97$ $Entropy(\text{High}) = -1/2 \cdot \log_2(1/2) - 1/2 \cdot \log_2(1/2) = 1$ $Entropy(\text{Normal}) = -2/3 \cdot \log_2(2/3) - 1/3 \cdot \log_2(1/3) = 0.92$ $Gain(\text{S, Humidity}) = 0.97 - (2/5) \cdot 1 - (3/5) \cdot 0.92 = 0.018$

Day 0	<u>Dutlook</u>	<u>Humid</u>	<u>Wind</u>
D4	Rain	High	Weak
D5	Rain	Normal	Weak
D6	Rain	Normal	Strong
D10	Rain	Normal	Weak
D14	Rain	High	Strong



 $Entropy(Wind) = -3/5 \cdot \log_2(3/5) - 2/5 \cdot \log_2(2/5) = 0.97$ $Entropy(Weak) = -3/3 \cdot \log_2(3/3) - 0/3 \cdot \log_2(0/3) = 0$ $Entropy(Strong) = -0/2 \cdot \log_2(0/2) - 2/2 \cdot \log_2(2/2) = 0$ $Gain(S, Wind) = 0.97 - (3/5) \cdot 0 - (2/5) \cdot 0 = 0.97$

<u>Day</u>	<u>Outlook</u>	<u>Humid</u>	<u>Wind</u>
D4	Rain	High	Weak
D5	Rain	Normal	Weak
D6	Rain	Normal	Strong
D10	Rain	Normal	Weak
D14	Rain	High	Strong



Decision Rule: Yes ⇔ (Outlook=Overcast) ∨ (Outlook=Sunny ∧ Humidity=Normal)∨ (Outlook=Rain ∧ Wind=Weak)

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Problems with Information Gain



All subsets perfectly pure \rightarrow optimal split

Information gain tends to favor attributes with lots of values.

We may use the notion of **Gain Ratio** = Gain(S,A)/ SplitEntropy(S,A). Mustafa Jarrar: Lecture Notes on **Decision Trees Machine Leaning** Birzeit University, 2021

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Overfitting in Decision Trees

- Can always classify training examples perfectly
 - keep splitting until each node contains 1 example
 - singleton = pure
- The more we split the the higher accuracy, but also the bigger the tree, the more specific decision tree.
- As a result: The decision tree will be too specific and accurate for the training data, but becomes less accurate for new data. Thus, the tree now not be able to classify data that didn't see before.
- In other words: the algorithm becomes too specific to the data we use to train it, and cannot generalize well to new data.
- This is called overfitting



Overfitting in Decision Trees

- Overfitting occurs when trying to model the training data perfectly.
- Overfitting means poor generalization.
- The test performance tells us how well our model generalizes, not the training performance
- ➔ Use Validation Test



Avoid Overfitting – Pruning

Try not to grow a tree that is too large to avoid overfitting. When to stop growing the tree?

Possible stopping (pre-pruning) criteria:

- Maximum depth reached
- Number of samples in each branch below certain threshold
- Benefit of splitting is below certain threshold.

Or we can grow a tree maximally then **post-prune** it.

this require a validation test

Avoid Overfitting – post-pruning

Creating the validation set



Be sure to have separate training, validation, and test sets

- Training set D_T , to build the tree
- Validation set D_{ν} to prune the tree
- Test set D_t to evaluate the final model.

Splitting of ($\frac{2}{3}$ training , $\frac{1}{3}$ testing) are common and best practice.

Testing data for later evaluation should not be used for pruning or you will not get honest estimate of the model's performance

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Avoid Overfitting – post-pruning

Prune the branches that will not do well on the future data

- Use validation set to get an error estimate E_T ,
- For each node *n* in the tree (pretend that all of its descendant nodes are pruned) then calculate the error $E_{T'}$ as if these nodes were deleted.
- Prune tree at the node that yields the highest error reduction.
- Repeat until further pruning is harmful.

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Continuous Attributes

Dealing with continuous-valued attributes: create a split: (Temperature > 72.3) = True, False

Threshold can be optimized (WF 6.1)



Continuous Attributes

Classifying Numerical values using Decision Trees This is like solving "regression problems" using Decision Trees:

- Regression algorithms can draw a boundary line between the data.
- Decision Trees are able to only make axisaligned splits of data. (only vertical and horizontal lines)
- Decision Trees introduces a threshold for each axis individually.
- But if keep introducing axis-aligned splits (the tree becomes bigger) and we end up overfitting.



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What is good about Decision Trees

- Interpretable: humans can understand decisions
- Easily handles irrelevant attributes (G=0)
- Very compact: #nodes << D after pruning
- Very fast at testing time: O(Depth)

Limitations for Decision Trees

- Greedy (may not find best tree).
- Instances are represented by attribute/value pairs(e., Outlook: sunny, Wind: strong), but what if we have discrete input values.
- The target function has discrete output values (e.g., Yes, No), thus we cannot have continues number output values.
- The training data may contain errors, or missing attributes
- Uncertainty in the data (e.g., suppose we have two exact days/features, one with "yes" and one with "no". → no classifier can help in such totally Uncertain data.

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Using R to learn Decision Trees

DT_example.R

Input.csv

Day,Outlook,Humidity,Wind,Play D1,Sunny,High,Weak,No D2,Sunny,High,Strong,No D3,Overcast,High,Weak,Yes D4,Rain,High,Weak,Yes D5,Rain,Normal,Weak,Yes D6,Rain,Normal,Strong,No D7,Overcast,Normal,Strong,Yes D8,Sunny,High,Weak,No D9,Sunny,Normal,Weak,Yes D10,Rain,Normal,Weak,Yes D11,Sunny,Normal,Strong,Yes D12,Overcast,High,Strong,Yes D13,Overcast,Normal,Weak,Yes D14,Rain,High,Strong,No require(C50) # the package that has the C5.0 decision tree require(gmodels) # a package used draw diagrams and graphs

```
print("Choose the data file when prompted")
dataset = read.table(file.choose(), header = T, sep=",")
# to exclude the DayNo column (column #1)
dataset = dataset[,-1]
```

apply the decision tree algorithm to the training data feature columns, and class column (output), and generate a DT Model. model = C5.0(dataset[, -4], dataset[, 4])

we plot the diagram of the generated decision tree plot(model, type="s", main="Decision Tree 1\n[%100 data used to train the model]")

Using R to learn Decision Trees



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by Jnan Morrar

Colab Link https://colab.research.google.com/drive/10g4gi5ifdqVLdv5QEY9GoSvo-A3eLCdy?usp=sharing

Mount Drive
from google.colab import drive
drive.mount("/content/drive")

[] from sklearn import tree #For our Decision Tree import pandas as pd # For our DataFrame import pydotplus # To create our Decision Tree Graph from IPython.display import Image # To Display a image of our graph

Read the input file.csv

data_inputs = pd.read_csv("/content/drive/My Drive/Ai Projects/Data/DataSheet.csv")
data_inputs.head() # print the first five values

	Day	Outlook	Humidity	Wind	Play
0	D1	Sunny	High	Weak	No
1	D2	Sunny	High	Strong	No
2	D3	Overcast	High	Weak	Yes
3	D4	Rain	Hiah	Weak	Yes Jarr

by Jnan Morrar

Colab Link https://colab.research.google.com/drive/10g4gi5ifdqVLdv5QEY9GoSvo-A3eLCdy?usp=sharing

Remove the day column from the input file

.

```
data_inputs = data_inputs.drop(["Day"] , axis = 1)
data_inputs.head()
```

	Outlook	Humidity	Wind	Play
0	Sunny	High	Weak	No
1	Sunny	High	Strong	No
2	Overcast	High	Weak	Yes
3	Rain	High	Weak	Yes
4	Rain	Normal	Weak	Yes

convert the categorical variables (Outlook, Humidity, Wind) into dummy/indicator variables or (binary variables) essentially 1's and 0's

] dummy_variables = pd.get_dummies(data_inputs[['Outlook', 'Humidity', 'Wind']]) dummy_variables.head()									
		Outlook_Overcast	Outlook_Rain	Outlook_Sunny	Humidity_High	Humidity_Normal	Wind_Strong	Wind_Weak	Wind_strong
	0	0	0	1	1	0	0	1	0
	1	0	0	1	1	0	1	0	0
	2	1	0	0	1	0	0	1	0
	3	0	1	0	1	0	0	1	0

by Jnan Morrar

Colab Link https://colab.research.google.com/drive/10g4gi5ifdqVLdv5QEY9GoSvo-A3eLCdy?usp=sharing

Remove the day column from the input file

.

[

```
data_inputs = data_inputs.drop(["Day"] , axis = 1)
data_inputs.head()
```

	Outlook	Humidity	Wind	Play
0	Sunny	High	Weak	No
1	Sunny	High	Strong	No
2	Overcast	High	Weak	Yes
3	Rain	High	Weak	Yes
4	Rain	Normal	Weak	Yes

convert the categorical variables (Outlook, Humidity, Wind) into dummy/indicator variables or (binary variables) essentially 1's and 0's

] dummy_variables = pd.get_dummies(data_inputs[['Outlook', 'Humidity', 'Wind']]) dummy_variables.head()									
		Outlook_Overcast	Outlook_Rain	Outlook_Sunny	Humidity_High	Humidity_Normal	Wind_Strong	Wind_Weak	Wind_strong
	0	0	0	1	1	0	0	1	0
	1	0	0	1	1	0	1	0	0
	2	1	0	0	1	0	0	1	0
	3	0	1	0	1	0	0	1	0

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Colab Link https://colab.research.google.com/drive/10g4gi5ifdqVLdv5QEY9GoSvo-A3eLCdy?usp=sharing

The decision tree classifier & Training the Decision Tree

```
[ ] clf = tree.DecisionTreeClassifier()
    clf_train = clf.fit(dummy_variables, data_inputs['Play']) # Training the Decision Tree
```

Double-click (or enter) to edit





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Colab Link https://colab.research.google.com/drive/10g4gi5ifdqVLdv5QEY9GoSvo-A3eLCdy?usp=sharing



References

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